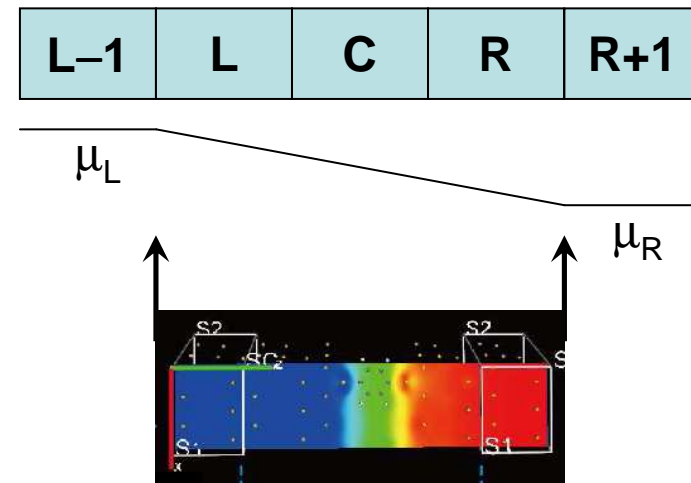
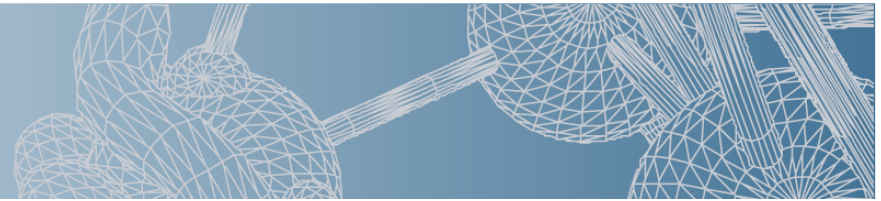


## Electrode Constraint, commonalities

- ❖ Determines the matching between the Hamiltonian  $H$ , density matrix (**DM**), real-space density  $\rho(r)$ , and effective potential  $V(r)$ 
  - » 1.  $H \rightarrow DM$  [Schrödinger]
  - » 2.  $DM \rightarrow \rho(r)$
  - » 3.  $\rho(r) \rightarrow V(r)$  [Poisson]
- ❖ Common:
  - »  $H$  in L(R) is always bulk-like (electrode calculation)
  - » **DM** in C is always computed from the Green's function
  - » The effective potential  $V(r)$  is matched at the boundaries of L+C+R to the bulk value
  - » Bias is applied over L+C+R
- ❖ 3 different constraints, with very different properties





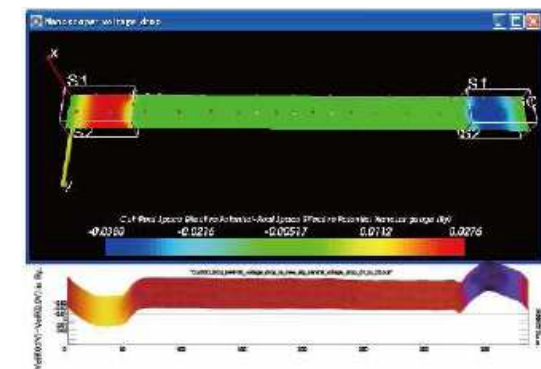
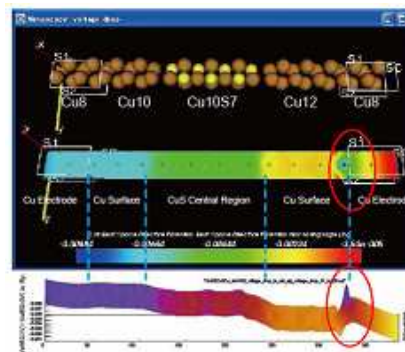
## “RealSpaceDensity”

## “Off”

- ❖ Original ATK constraint
- ❖  $\rho(r)$  in L/R is constrained to the bulk density
- ❖ **Good**, because this matches H in L/R
- ❖ **Bad**, DM does not match  $\rho(r)$  in L/R
- ❖ **Worse**, if there is insufficient screening the density can become discontinuous
  - » Which in turns leads to other problems...
- ❖ **Exactly correct** in the limit of infinitely many screening layers
- ❖ Can give bad **voltage drop** → depending on atom positions in the electrode
  - » Can be solved by centering the electrode atoms

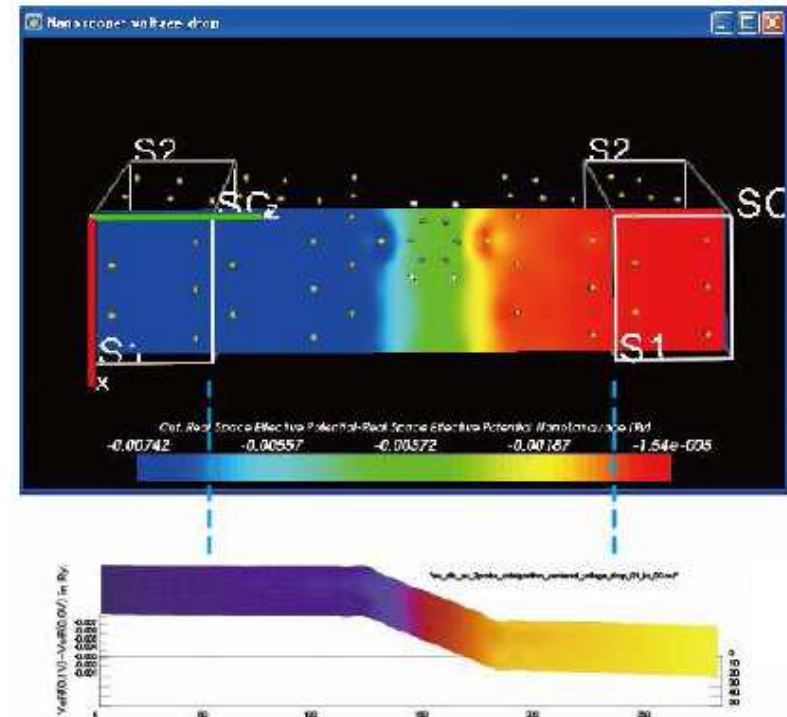


- ❖ **Default** since ATK 2008.02
- ❖ Allows DM and  $\rho(r)$  in L/R to vary freely, self-consistently
- ❖ Forgiving in cases of few screening layers
- ❖ **Good**: Continuous density (and  $\rho(r)$  matches DM)
- ❖ **Bad**:  $\rho(r)$  and hence  $V(r)$  does not match H (and DM is missing some contributions)
- ❖ Therefore, “Off” cannot produce a correct **voltage drop** ↴



## “DensityMatrix”

- ❖ Partially undocumented, introduced in 2008.10
- ❖ Not available from VNL
  - » Was initially not 100% tested
- ❖ Appears to be the best constraint of all 3
  - » Except some points, see below
- ❖ DM in L/R is constrained to bulk values
- ❖  $\rho(r)$  is computed self-consistently
- ❖ **Good**, because DM matches H in L/R
- ❖ **Even better**, the density is continuous
- ❖ **Exactly correct** in the limit of infinitely many screening layers
- ❖ **Less good**:
  - » Slower
  - » Less forgiving if screening is insufficient (convergence failure)
- ❖ **Best**: The *only* constraint that consistently can give a good voltage drop





## Note

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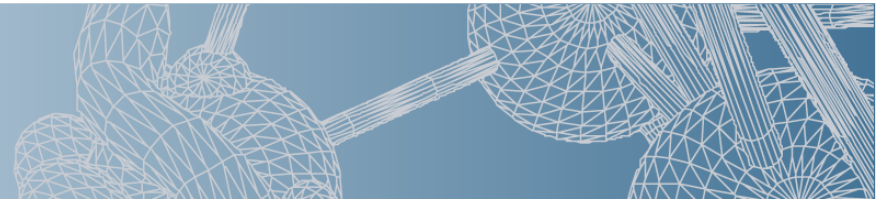
❖ Transmission spectrum and current appear to be quite insensitive to the constraint



» Provided the calculation converges...




» Partly an assumption, not tested in all cases...



## Is “DensityMatrix” the end of the story?



- ❖ No
  - ❖ Next version of ATK will use a different separation of L/C/R, which does away with the need for a specified constraint completely
  - ❖ All quantities, from  $H$  to  $V(r)$ , will be treated fully self-consistently in the region over which the bias is applied ( $C^*$ )
  - ❖ Effectively this means the user must now include L and R explicitly in  $C^*$ , thus  $C^*=L+C+R$
  - ❖ Fully consistent approach
    - » Continuous density
    - » Consistency between  $H$ ,  $DM$ ,  $\rho(r)$ , and  $V(r)$  in  $C^*$
    - » Correct voltage drop
- 
 “Screening approximation” still necessary
  - » Match to bulk at edges of  $C^*$

